

## Subject Description Form

<b>Subject Code</b>	COMP2014							
<b>Subject Title</b>	Mathematics for Machine Learning							
<b>Credit Value</b>	3							
<b>Level</b>	2							
<b>Pre-requisite / Co-requisite / Exclusion</b>	NIL							
<b>Objectives</b>	<p>The objectives of this subject are to:</p> <ul style="list-style-type: none"> <li>• provide the basic concepts of mathematics for machine learning</li> <li>• apply practical problem-solving skills by using appropriate numerical computing environments and mathematical software libraries</li> </ul>							
<b>Intended Learning Outcomes</b>	<p>Upon completion of the subject, students will be able to:</p> <p><u>Professional/academic knowledge and skills</u></p> <p>(a) understand the basic concepts of mathematics for machine learning;</p> <p>(b) apply proper mathematics concepts in solving problems;</p> <p>(c) familiarize with numerical computing environments and mathematical software libraries;</p> <p><u>Attributes for all-roundedness</u></p> <p>(d) solve problems independently; and</p> <p>(e) think critically for improvement in solutions.</p>							
<b>Subject Synopsis/ Indicative Syllabus</b>	<table border="1" style="width: 100%; border-collapse: collapse;"> <thead> <tr> <th style="text-align: left; padding: 5px;"><b>Topic</b></th> <th style="text-align: center; padding: 5px;"><b>Duration of Lectures</b></th> </tr> </thead> <tbody> <tr> <td style="padding: 5px;"> <b>1. Numerical computing software</b>            Mathematical software libraries (e.g., Numpy, Pandas, Scikit-Learn; numerical computing environments (e.g., Pytorch, Keras, Matlab)         </td> <td style="text-align: center; padding: 5px;">4</td> </tr> <tr> <td style="padding: 5px;"> <b>2. Linear algebra</b>            Vector space; linear transformation and matrices; solving linear equations; matrix decomposition; eigenvalues and singular values; matrix norms and condition numbers; inverse matrices; column space and null space; non-square matrices as transformation between dimensions; pseudo-inverses         </td> <td style="text-align: center; padding: 5px;">12</td> </tr> </tbody> </table>		<b>Topic</b>	<b>Duration of Lectures</b>	<b>1. Numerical computing software</b> Mathematical software libraries (e.g., Numpy, Pandas, Scikit-Learn; numerical computing environments (e.g., Pytorch, Keras, Matlab)	4	<b>2. Linear algebra</b> Vector space; linear transformation and matrices; solving linear equations; matrix decomposition; eigenvalues and singular values; matrix norms and condition numbers; inverse matrices; column space and null space; non-square matrices as transformation between dimensions; pseudo-inverses	12
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	<b>3. Optimization</b> One-dimensional optimization; least squares; constrained optimization; convex optimization; gradient descent; stochastic gradient descent	4																																																									
	<b>4. Probability and Statistics</b> Recap of basic concepts in probability; maximum likelihood estimation; Bayes' rule; statistical inference	4																																																									
	<b>5. Applications of mathematical skills in machine learning</b> Linking mathematical skills with machine learning problems; examples of applications of mathematical skills in machine learning; the relevance to the machine learning subjects in COMP	2																																																									
	<b>Total</b>	<b>26</b>																																																									
<b>Teaching/ Learning Methodology</b>	<p>Lectures provide students with the main concepts of the topic, together with comprehensive examples for easy understanding.</p> <p>Tutorial and lab sessions offer an opportunity to students for practicing their skills.</p> <p>Both written and programming assignments will be utilized in the course. Written assignments help students develop theoretical skills, whereas programming assignments emphasize on practical skills.</p>																																																										
<b>Assessment Methods in Alignment with Intended Learning Outcomes</b>	<table border="1" style="width: 100%; border-collapse: collapse;"> <thead> <tr> <th rowspan="2" style="width: 25%;">Specific assessment methods/tasks</th> <th rowspan="2" style="width: 10%;">% weighting</th> <th colspan="5">Intended subject learning outcomes to be assessed (Please tick as appropriate)</th> </tr> <tr> <th style="width: 8%;">a</th> <th style="width: 8%;">b</th> <th style="width: 8%;">c</th> <th style="width: 8%;">d</th> <th style="width: 8%;">e</th> </tr> </thead> <tbody> <tr> <td colspan="7"><b>Continuous Assessment</b></td> </tr> <tr> <td>1. Written assignments</td> <td>20%</td> <td style="text-align: center;">✓</td> <td style="text-align: center;">✓</td> <td></td> <td style="text-align: center;">✓</td> <td style="text-align: center;">✓</td> </tr> <tr> <td>2. Programming assignments</td> <td>15%</td> <td style="text-align: center;">✓</td> <td style="text-align: center;">✓</td> <td style="text-align: center;">✓</td> <td style="text-align: center;">✓</td> <td style="text-align: center;">✓</td> </tr> <tr> <td>3. Quizzes</td> <td>25%</td> <td style="text-align: center;">✓</td> <td style="text-align: center;">✓</td> <td></td> <td style="text-align: center;">✓</td> <td style="text-align: center;">✓</td> </tr> <tr> <td><b>Examination</b></td> <td>40%</td> <td style="text-align: center;">✓</td> <td style="text-align: center;">✓</td> <td></td> <td style="text-align: center;">✓</td> <td style="text-align: center;">✓</td> </tr> <tr> <td>Total</td> <td>100%</td> <td></td> <td></td> <td></td> <td></td> <td></td> </tr> </tbody> </table> <p>Both written assignments and quizzes are mainly used to assess the understanding of mathematics concepts and their applications to machine learning problems, i.e., the outcomes (a) and (b).</p> <p>Quizzes are expected to be short and conducted in class. In contrast, written assignments may cover both short questions and long questions.</p> <p>Programming assignments are mainly used to assess implementation skills, i.e., the outcome (c).</p>					Specific assessment methods/tasks	% weighting	Intended subject learning outcomes to be assessed (Please tick as appropriate)					a	b	c	d	e	<b>Continuous Assessment</b>							1. Written assignments	20%	✓	✓		✓	✓	2. Programming assignments	15%	✓	✓	✓	✓	✓	3. Quizzes	25%	✓	✓		✓	✓	<b>Examination</b>	40%	✓	✓		✓	✓	Total	100%					
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	All assessment tasks are relevant to outcomes (d) and (e), i.e., independent problem-solving and critical thinking for improvements.	
<b>Student Study Effort Expected</b>	Class contact:	
	▪ Lecture	26 Hrs.
	▪ Tutorial/Lab	13 Hrs.
	Other student study effort:	
	▪ Assignments, Quizzes, Self-study	66 Hrs.
	Total student study effort	105 Hrs.
<b>Reading List and References</b>	<b>Reference Books:</b> <ol style="list-style-type: none"> <li>1. Marc Peter Deisenroth, A. Aldo Faisal, and Cheng Soon Ong: Mathematics for Machine Learning, Cambridge University Press, 2020. PDF: <a href="https://mml-book.github.io/">https://mml-book.github.io/</a></li> <li>2. Trevor Hastie, Jerome H. Friedman, Robert Tibshirani: The Elements of Statistical Learning: Data Mining, Inference, and Prediction. Second Edition, Springer Series in Statistics, Springer 2001. PDF: <a href="https://hastie.su.domains/Papers/ESLII.pdf">https://hastie.su.domains/Papers/ESLII.pdf</a></li> <li>3. Ian Goodfellow and Yoshua Bengio and Aaron Courville: Deep Learning, MIT Press, 2016.</li> <li>4. Christopher Bishop: Pattern Recognition and Machine Learning, 5th Edition. Information science and statistics, Springer 2007</li> <li>5. A. Quateroni, F. Saleri, and P. Gervasio: Scientific Computing with MATLAB (Texts in Computational Science and Engineering, 2), 4<sup>th</sup> Edition, Springer 2014.</li> </ol>	