# AE8104 Finite Element Analysis of Composites (3 credits)

Fall 2022 Class time: TBD, East Middle Hall 4-301 https://oc.sjtu.edu.cn/courses/36842

#### **Course objective:**

This course aims at providing fundamental and practical notions in finite element analysis. The course will present systematic approaches for the derivation of various finite elements. The students will also be introduced to numerical techniques for the solution of the discretized governing equations. Practical aspects such as mesh generation and choice related to numerical integration will also be presented. This course will mostly be based on structural analysis, focusing on both isotropic and composite materials. Students need to program their own FE code to accomplish homework and final project.

#### **Instructors:**

Yile Hu yilehu@sjtu.edu.cn office A430

## TA:

Jiaming Liang	liangjiaming_6@sjtu.edu.cn	
Dahua Hao	haodahua@sjtu.edu.cn	

# **Office Hours:**

To be determined.

## **Textbook:**

- 1. Class Notes;
- 2. Finite Element Analysis of Composite Materials, Ever J. Barbero;
- 3. The Finite Element Method: Its Basis & Fundamentals 7th Edition, O.C.Zienkiewicz.

## **Prerequisites:**

Student should have previous knowledge or currently registered to courses: Solid Mechanics, Mechanics of Composites, Linear Algebra, and Numerical analysis. Moreover, this course requires some programming knowledge with C/C++, FORTRAN, Java, Python or any other computer language you prefer. Matlab is not recommended for graduate students.

## **Grade Policy:**

Letter grade's policy is subjected to SJTU policy: A+ [95, 100], A [90, 95), A- [85, 90); B+ [82, 85), B [78, 82), B- [75, 78); C+ [71, 75), C [67, 71), C- [63, 67); D [60, 63), F [0, 60).

Homework 30%, Quiz 10% (two quiz), Midterm exam 30%, Final project 30%.

## **Class Policy:**

1. Class attendance is mandatory. If a student is absent, proper documented justification is required;

- **2.** All holidays or special events observed by organized religious will be honored for those students who show affiliation with that particular religion;
- **3.** Professional behavior is expected in this course. Cell phone, laptop and tablet should be turned off unless for class needed.

#### Policies against plagiarism:

- 1. Homework and final project: if there is evidence that a student has copied some solution material (from another student and/or a manual), grade zero will be assigned to this particular homework (project);
- 2. Midterm exam and quiz: If a student is caught taking information or passing information from or to another student during an exam, grade zero will be assigned to the exam (quiz).

#### **Students with Disabilities:**

If you anticipate issues related to the format or requirements of this course, please meet with me. I would like us to discuss ways to ensure your full participation in the course. If you determine that formal, disability-related accommodations are necessary, it is important that you notify me of your eligibility for reasonable accommodations. We can then plan how best to coordinate your accommodations.

# Class Agenda (Tentative):

Week	Content	Dates
	Syllabus	
	Chapter I. Introduction	
1	Chapter II. Construction of FE equations	Sept 24
	- Minimization of potential energy;	
	- Rayleigh-Ritz method;	
	- Galerkin method;	
	- Variational approach.	
2	Chapter III. One-Dimensional Problem	Oct 8
-	3.1. 2-noded truss element	
	- Shape functions;	
	- Coordinate transformation;	
	<ul> <li>Assemble global stiffness matrix;</li> </ul>	
3	- Boundary conditions;	Oct 15
	- Reduced stiffness matrix;	00015
	- Calculate nodal and elemental variables.	
	3.2. 3-noded truss element	
	- Elemental stiffness matrix;	
4	<ul> <li>Coordinate transformation.</li> </ul>	Oct 22
	3.3. Multi-Point Constraints (MPC)	
	Quiz	
	Chapter IV. Two-Dimensional Problem	
	4.1. Constant Strain Triangle (CST) element	
	<ul> <li>Parent coordinate system;</li> </ul>	
5	<ul> <li>Approximated solution;</li> </ul>	Oct 29
5	- Shape function;	001 29
	- Jacobian matrix;	
	<ul> <li>Jacobian matrix,</li> <li>Elemental stiffness matrix;</li> </ul>	
	<ul> <li>Equivalent nodal force.</li> </ul>	
	4.2. Bilinear quadrilateral element	
	<ul> <li>Parent coordinate system;</li> </ul>	
	- Approximated solution;	
	- Shape function;	
6	- Elemental stiffness matrix;	Nov 5
	- Numerical integration;	
	- Equivalent nodal force;	
	- Stress and strain extraction.	
	4.3. Shear locking and hourglass mode	
	4.5. Shear locking and hourglass mode 4.4. Pascal's triangle	
	4.4. Fascal's triangle 4.5. Quadratic triangle element	
7	4.6. Quadratic quadrilateral element	Nov 12
	4.7. 9-noded quadrilateral element	
	4.8. Axisymmetric Problem	
	Chapter V. Three-Dimensional Problem	
	5.1. 4-noded tetrahedral element	
8	5.2. 10-noded tetrahedral element	
	5.3. 8-noded hexahedral element	
	- Selectively Reduced Integration (SRI);	Nov 19
	<ul> <li>Selectively Reduced Integration (SRI),</li> <li>Equivalent nodal force.</li> </ul>	1101 19
	5.4. 20-noded hexahedral element	
	- 14-Points Rule (14PR);	
	- Equivalent nodal force.	
	· · · · · · · · · · · · · · · · · · ·	
9	Midterm exam	TBD

	Chapter VI. Solution Technique	
	6.1. Gauss elimination	
	6.2. LU decomposition	
	6.3. LDL <sup>T</sup> decomposition	
	6.4. Conjugate Gradient method	
10	- CG algorithm;	No. 26
10	- Preconditioned CG algorithm;	Nov 26
	- Choice of preconditioner.	
	6.5. Generalized Minimal Residual method	
	- Krylov subspace;	
	- GMRes algorithm;	
	- Preconditioned GMRes algorithm.	
	6.6. Convergence analysis	
	Chapter VII. Structural Element	
	7.1. Euler-Bernoulli beam element	
	- Beam theory;	
	- Governing equation;	
11	- Galerkin's method;	Dec 3
	- Shape function;	
	- Elemental stiffness matrix;	
	- Coordinate transformation;	
	- Equivalent nodal force.	
	7.2. Timoshenko beam element	
	- Shape function;	
	- Elemental stiffness matrix.	
	7.3. Nonconforming plate element	
12	- Plate theory;	Dec 10
	- $C_1$ continuity;	
	- Shape function;	
	- Elemental stiffness matrix;	
	- Equivalent nodal force.	
	7.4. Conforming plate element	
	- Shape function;	
13	- Elemental stiffness matrix;	Dec 17
	- Equivalent nodal force;	
	- Mixed interpolation for transverse shear strains.	
	Quiz	
	Chapter VIII. Modeling Macromechanical Structures of Composites	
14	8.1. Modeling composite laminate with shell element	Dec 24
	8.2. Modeling composite laminate with solid element	
	8.3. Failure criteria and continuum damage mechanics	
15	Chapter IX. Modeling Micromechanical Structures of Composites	De: 21
15	9.1. Continuous fiber reinforced composites	Dec 31
	9.2. Short fiber reinforced composites	
	Chapter X. Dynamic and Buckling Analyses	
16	10.1. Linear buckling analysis	
	10.2. Derivation of mass matrices	Jan 7
	10.3. Computation of eigenvalues and mode shapes	
L	2010. Sompation of eigen , made and mode shapes	